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# Reasoning the Fast and Frugal Way: Models of Bounded Rationality

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## Reasoning the Fast and Frugal Way: Models of Bounded Rationality

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Humans and animals make inferences about the world under limited time and knowledge. In contrast, many models of rational inference treat the mind as a Laplacean Demon. equipmed with un-

limited time, knowledge, and computational might. Following H. Simon's notion of satisficine, the

#### REASONING THE FAST AND FRUGAL WAY

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ea	would suggest that the mind is a supercalculator like a Lapla-	'reasonableness' " (p. 78). They did not report such a test. We
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-	cean <u>Demon (Wimsatt, 1976)</u> —carrying around the collected	shall.
	works of Kolmogoroff. Fisher. or Nevman—and simply needs a	Initially, the concept of bounded rationality was only vaguely
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	memory jog, like the slave in Plato's Meno. On the other hand, the beuristics-and-biases view of human irrationality would	defined, often as that which is not classical economics, and one could "fit a lot of things into it by foresight and hindsight." as
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÷	<u>could be based</u> , that is, knowledge is limited. We model limited	Object a	
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		positive	
, <b>E</b>	knowledge in two respects: A person can have (a) incomplete		
	z	Object b unknown	
	knowledge of the objects in the reference class (e.g., she recog-		
		negative	
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	values (facts about cities), or (c) both. For instance, a person		
<del></del>	who does not know all of the cities with soccer teams may know	· · · · · · · · · · · · · · · · · · ·	
	some cities with positive cue values (e.g., Munich and Hamburg		
	certainly have teams). many with negative cue values (e.g., Hei-		
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č <b></b> -	delberg and Potsdam certainly do not have teams), and several		_
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	<u><b>Gues.</b> Ecological Validities</u> , and Discrimination Rates	tant for Simon's postulated link between the cognitive and the
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	Table 1	adra time and commutational neuron This question is import

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	variation betwee	n recognition of cities and city populations. Let	-8	.8
	us define the va	<i>lidity</i> $\alpha$ of the recognition principle to be the	ł	1
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	predictors or cues and is commonly seen as an "optimal" way 4 cue values (that is, one fifth of all possible) are searched for.
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	Brunswik, 1955; Hammond, 1966). Neural networks using the less than a third of all available cue values.
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delta rule determine their "optimal" weights by the same prin-

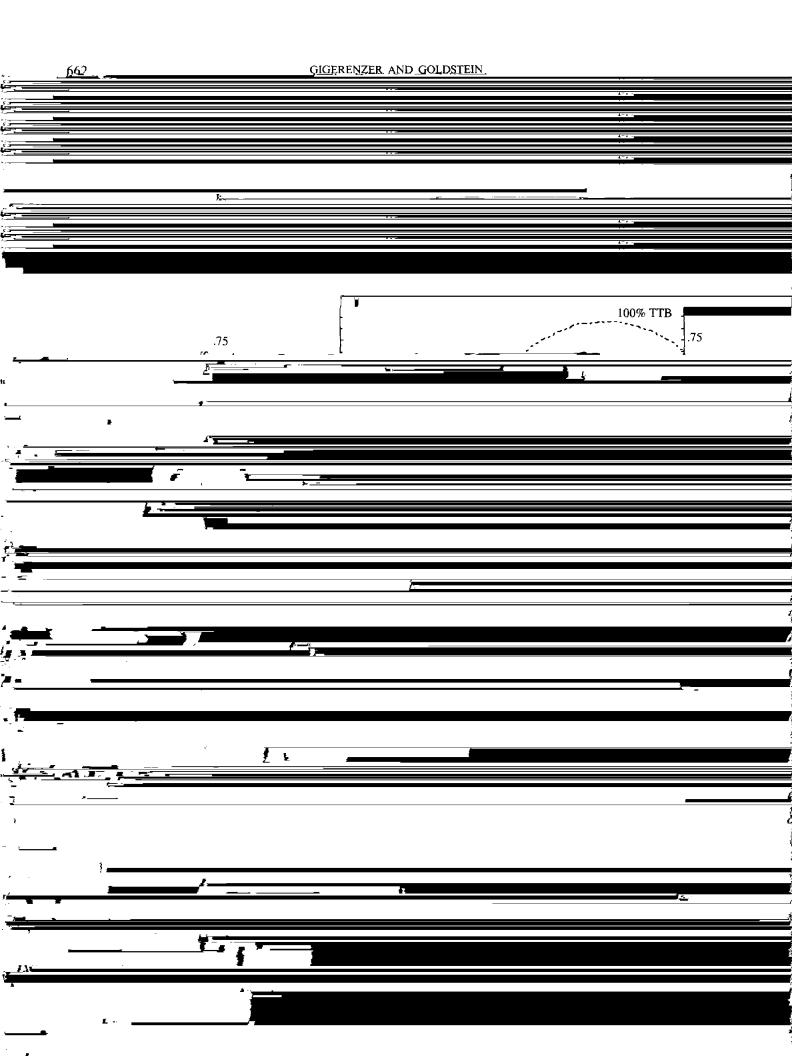
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· ·	Results of the Competition: Average Proportion_	A 7 28	Here the unit-weight a	and weighted linear m	odels often make	
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,	of Correct Inferences		the inference that the u	nrecognized object is t	he larger one due	
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rithm then tries the cue that discriminated the time before last.	smaller and smaller. The reason why the Minimalist algorithm
and so on. The algorithm differs from the Take The Best algo-	looks up fewer cue values than the Take The Best algorithm is
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rithm in Step 2, which is now reformulated as Step 2':	that cue validities and cue discrimination rates are negatively
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	correlated (Table 1); therefore, randomly chosen cues tend to
Ston 2' Search for the Cue Values of the	have larger discrimination rates than cues chosen by cue



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	ative to the PMM family of satisficing algorithms is the lexico-	great topic but does not recognize the name of the author, he
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	<u></u>	makes the inference that it is probably not worth buying. If,
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	summary see Lopes. 1995). However, despite empirical evi-	of the names. he concludes the book is not even worth reading.
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disjunctive algorithms (	Einhorn, 1970) and highly comm	lex	<u> </u>	<u>^</u>	
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	ine three species: <i>a</i> , <i>b</i> , and <i>c</i> . Species <i>a</i> inhabits both water and	New <u>Perspective on</u> the <u>L</u>		<i>k</i>

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## REASONING THE FAST AND FRUGAL WAY

City	Population	Soccer team	State capital	Former East Germany	Industrial belt	Licence plate	Intercity trainline	Exposition site	National capital	University
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<u>Mainz</u>	179, <u>486</u>		+	_	-	-	+	-		ł
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Herne Mülheim	178,132 177,681		-		+ +	_		_		
Solingen	165,401		_	-	т —	_	+	_	_	-
Osnabrück Ludwigshafen	163,168 162,173	_	-	_	-	_	+ +	-	_	+ _
Leverkusen	160.919	+						_	_	_
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Qldenburg	143.131		-		_	-	+		_	+
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Darmstadt	138,920		_	_	_	_	+	_		+
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